

Rules of Divisibility

Divisible by:	Test	Example
2	Last digit is even (=0, 2, 4, 6, or 8)	3,489,076: Last digit = 6 (even) $6 = 3 \times 2$
3	<ol style="list-style-type: none"> The sum of the digits of the number is divisible by 3 Can repeat until sum is 2-digit number that is/not recognizably divisible by 3 	16,499,205,854,376: $1 + 6 + 4 + 9 + 9 + 2 + 0 + 5$ $+ 8 + 5 + 4 + 3 + 7 + 6 = 69$ $6 + 9 = 15$ $15 = 5 \times 3$
4	<ol style="list-style-type: none"> Last 2 digits are divisible by 4 Tens digit is even and the ones digit = 0, 4, or 8 Tens digit is odd and the ones digit = 2 or 6 	358,912: <ol style="list-style-type: none"> Last 2 digits = 12 $12 = 3 \times 4$ Tens digit = 1, odd & ones digit = 2
5	Last digit is 5 or 0	3,783,953,495: Last digit = 5
6	Divisible by 2 (even) and 3	57,342 Last digit = 2 (even) and $5 + 7 + 3 + 4 + 2 = 21$, divisible by 3
7	Double the last digit, then subtract the result from the rest of the digits. Repeat for larger numbers until result is a 2-digit number; 2-digit number is divisible by 7	357: $2 \times 7 = 14$ (double the last digit) $35 - 14 = 21$ (subtract) $21 = 3 \times 7$
8	<ol style="list-style-type: none"> Hundreds digit even: last 2 digits divisible by 8 Hundreds digit odd: add 4 to the last 2 digits and sum is divisible by 8 Last 3 digits divisible by 8 	986,104: <ol style="list-style-type: none"> Hundreds digit = 1, odd $04 + 4 = 8$ Last 3 digits = 104 $104 = 13 \times 8$
9	The sum of the digits of the number is divisible by 9	24,343,785: $2 + 4 + 3 + 4 + 3 + 7 + 8 + 5 = 36$ $36 = 4 \times 9$
10	Last digit is 0	34,789,013,467,593,487,540: Last digit = 0
11	<ol style="list-style-type: none"> Alternately subtract, then add the digits from L to R; the sum is divisible by 11 Subtract the last digit from the rest 	918,082: <ol style="list-style-type: none"> $9 - 1 + 8 - 0 + 8 - 2 = 22$ $22 = 2 \times 11$ 627: <ol style="list-style-type: none"> $62 - 7 = 55$ $55 = 5 \times 11$

Divisible by:	Test	Example
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12	Divisible by 3 and 4	324: $3 + 2 + 4 = 9$, divisible by 3 and Last 2 digits = 24, divisible by 4
13	Add 4 times the last digit to the rest of the digits. Repeat until sum is/not recognizably divisible by 13	637: $63 + (7 \times 4) = 91$ $9 + (1 \times 4) = \mathbf{13}$
14	Divisible by 2 and 7	182: Last digit = 2 (even), divisible by 2 and $2 \times 2 = 4$ (double the last digit) $18 - 4 = 14$, divisible by 7
15	Divisible by 3 and 5	345: $3 + 4 + 5 = 12$, divisible by 3 and Last digit = 5, divisible by 5
16	<ol style="list-style-type: none"> Thousands place even: take the last 3 digits Thousands place odd: add 8 to the last 3 digits With the 3-digit number: multiply hundreds digit by 4, then add the last 2 digits 	254,176: Thousands digit = 4, so 176 $(1 \times 4) + 76 = 80$ $80 = 5 \times \mathbf{16}$ 693,408: Thousands digit = 3, so $408 + 8 = 416$ $(4 \times 4) + 16 = 32$ $32 = 2 \times \mathbf{16}$
17	Subtract 5 times the last digit from the rest	221: $22 - (1 \times 5) = \mathbf{17}$
18	Divisible by 2 and 9	35,406: Last digit = 2 (even), divisible by 2 and $3 + 5 + 4 + 0 + 6 = 18$, divisible by 9
19	Add twice the last digit to the rest	437: $43 + (7 \times 2) = 57$ $5 + (7 \times 2) = \mathbf{19}$
20	Divisible by 10 and the tens digit is even	360: Last digit = 0 and tens digit = 6 is even
25	Last 2 digits are 25, 50, or 75	895,438,675: Last 2 digits = 75 7,325: Last 2 digits = 25
50	Last 2 digits are 50 or 00	686,352,400: Last 2 digits = 00 327,950: Last 2 digits = 50